Geometric functions normally live in Flatland. In this lesson you will take them to visit Numberland. The lesson is here: <u>geometricfunctions.org/fc/unit4/flatland-to-numberland/</u>

# WARMUP

In the Warmup activity your task is to find two different ways to help the Reflect function get into Lineland together, without leaving the dependent variable outside.

- 1. For sketch page 1, describe how you adjusted the mirror to get  $r_m(x)$  into Lineland.
- 2. For sketch page 2, describe another way to get  $r_m(x)$  into Lineland, and explain how the two ways are similar and how they're different.

# INTRODUCE

There's a novel and several movies about adventures in Flatland, including a trip to Lineland.

# **REDUCE THE DIMENSION**

On each page of the sketch, follow the construction directions under the sketch.

## Sketch Page 1 (Reflect):

- 3. Does  $r_m(x)$  stay in Lineland as you vary x?
- 4. How does  $r_m(x)$  move in relation to x?
- 5. What happens when you change the function rule by dragging *P* and *Q*?

#### Sketch Page 2 (Rotate):

- 6. Does  $R_{C,\theta}(x)$  stay in Lineland as you vary x?
- 7. How does  $R_{C,\theta}(x)$  move in relation to x?

8. What happens when you change the function rule by dragging *C* and  $\theta$ ?

#### Sketch Page 3 (Translate):

- 9. Does  $T_v(x)$  stay in Lineland as you vary x?
- 10. How does  $T_v(x)$  move in relation to x?

11. What happens when you change the function rule by dragging the vector endpoints?

#### Sketch Page 4 (Dilate):

- 12. Does *D<sub>C,s</sub>(x)* stay in Lineland as you vary *x*?
- 13. How does  $D_{C,s}(x)$  move in relation to x?

14. What happens when you change the function rule by dragging *C* and *s*?

#### Sketch Page 5 (Glide Reflect):

15. Does  $G_v(x)$  stay in Lineland as you vary x?

- 16. How does  $G_{\nu}(x)$  move in relation to x?
- 17. What happens when you change the function rule by dragging the vector endpoints?

#### Summarize:

18. Which families have the most interesting experiences? Explain.

# NUMBER THE DOMAIN

# Sketch Page 1 (Reflect):

19. Describe what you notice about the values in a sentence or two.

20. Use mathematical symbols to summarize your description.

21. Why do you think this happens? Explain.

## Sketch Page 2 (Rotate):

22. Describe what you notice about the values in a sentence or two.

23. Use mathematical symbols to summarize your description.

24. Why do you think this happens? Explain.

## Sketch Page 3 (Translate):

25. Describe what you notice about the values in a sentence or two.

26. Use mathematical symbols to summarize your description.

27. Why do you think this happens? Explain.

### Sketch Page 4 (Dilate):

28. Describe what you notice about the values in a sentence or two.

29. Use mathematical symbols to summarize your description.

30. Why do you think this happens? Explain.

#### Sketch Page 5 (Glide Reflect):

31. Describe what you notice about the values in a sentence or two.

32. Use mathematical symbols to summarize your description.

33. Why do you think this happens? Explain.